

# Analysis, design and control of a resonant forward-flyback converter

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**Abstract**—A resonant forward-flyback converter is proposed in this paper, in which the high efficiency resonant forward part delivers most of the power and the flyback part achieves tight regulation and magnetic resetting. Operating characteristics are analyzed in detail. As the key design parameters, this paper studies the influence of transformer’s turns-ratios on component stress and power loss. A minimum duty cycle control strategy ( $D_{min-fs}$ ) is proposed to guarantee ZCS of forward diode and valley switching. An experimental prototype of 400V input 48V output is built to verify the analysis. The prototype achieves a high efficiency of 96% at 120W output.

**Keywords**—resonant forward; valley switching;  $\Sigma$  /sigma topology;

## I. INTRODUCTION

High power density and high efficiency are two key elements of the DC/DC converter design. Due to the simple structure, high efficiency and low EMI characteristics, resonant converters such as LLC converters, resonant forward converters, have been widely used in server power supply, EV chargers and other applications[1]-[7]. A lot of researches have been made to further improve the performance of resonant converters. To reduce the volume of magnetics, the integration of the resonant inductor into the transformer has been introduced in LLC resonant converters [6]. Different integrated magnetic structures are proposed, investigated and compared so as to obtain higher efficiency and power density. Resonant forward converter is another promising resonant topology featuring compactness and zero current switching in the rectifier[7]. In [7], the quasi-ZVS turn-on and quasi-ZCS turn-off are both achieved and the high voltage stress in the traditional resonant forward converter is reduced by secondary diode-clamping. Some resonant converters have their optimum operation point with very high efficiency and load-independent output characteristics. Therefore, it is also an effective method to combine the converters operating at the optimum operation point with another converter together to achieve high efficiency and tight regulation simultaneously, i.e.  $\Sigma$  /sigma topology concept. In paper [4]-[5], the LLC DCX was combined with Input-series Output-parallel Flyback circuit

with  $\Sigma$  /sigma topology concept. Most power was transmitted by LLC DCX and the Flyback was responsible for voltage regulation.

According to the concepts of  $\Sigma$  /sigma topology and magnetic integration, this paper proposes a resonant forward-flyback converter and analyzes its working principle. Both ZCS condition of forward diode and output voltage characteristic are derived in this paper. This paper conducts a study of the influence of transformer turns ratios on converter characteristics and gives the design basis of turns ratio from the view of efficiency optimization. Finally, this paper will present the control strategy of the system and carry out corresponding experiments to verify the theoretical analysis.

## II. ANALYSIS OF THE PROPOSED RESONANT FORWARD-FLYBACK CONVERTER

### A. Proposing of the resonant forward-flyback converter

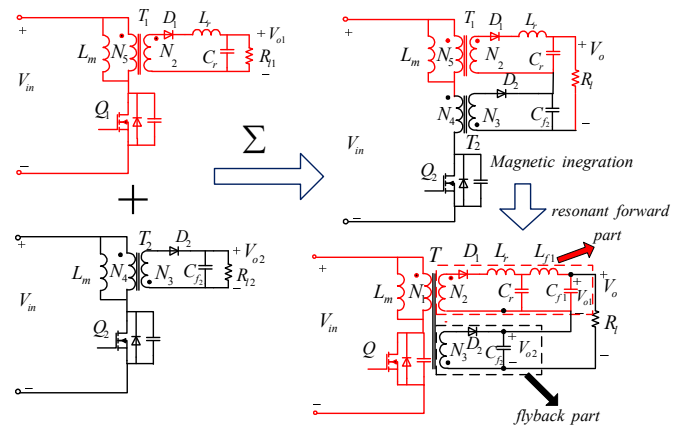


Fig.1 Resonant forward-flyback converter

Fig.1 shows the proposing of the resonant forward-flyback converter: Combining resonant forward converter with flyback converter using the concept of  $\Sigma$  /Sigma topology and applying magnetic integration, as shown in Fig.1, the resonant

forward-flyback converter can then be obtained. Where  $N_1, N_2, N_3, D_1, D_2, L_m, L_r, C_r$  and  $Q$  represent primary turns, resonant forward part turns, flyback part turns, forward diode, flyback diode, magnetizing inductor, leakage inductor, resonant capacitor and switch respectively.

### B. Characteristics analysis

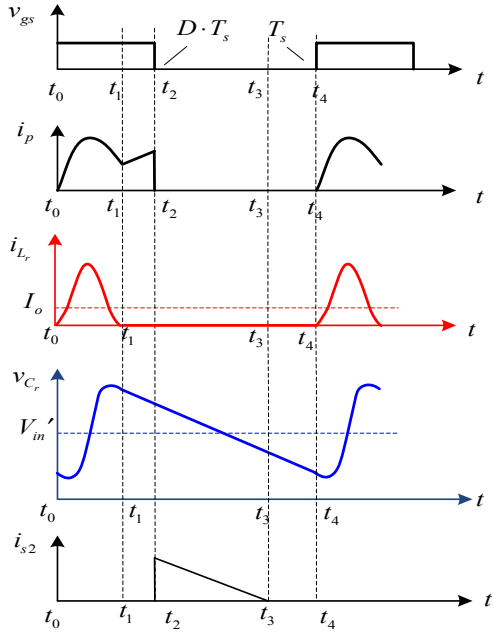


Fig.2(a)Key waveforms in FR-DCM mode

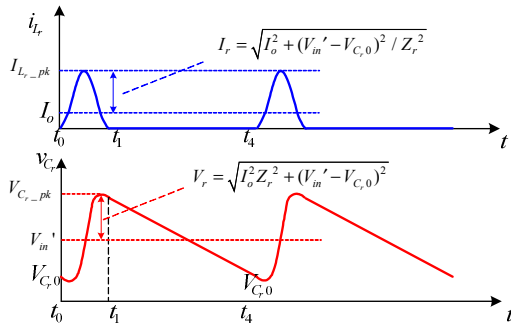


Fig.2(b) Key waveforms of the resonant forward part

There are several operation mode combinations for resonant forward part and flyback part. Forward part can operate in full resonant mode (FR) or partial resonant mode (PR), and flyback part can in DCM mode or CCM mode. In order to realize the ZCS for  $D_1$  and valley switching for  $Q$ , the converter should work in FR-DCM mode which means forward part operates in FR and flyback part in DCM. Accordingly, only the key waveforms of the proposed converter in FR-DCM are given in Fig. 2(a).

To better understand the operating principle of the proposed converter, the operation mode of FR-DCM is briefly analyzed here.

Mode 1 [ $t_0$ - $t_1$ ]: When  $Q$  turns on at  $t_0$ , forward diode  $D_1$  is conducting, leakage inductor  $L_r$  begins to resonant with resonant capacitor  $C_r$  and satisfied the resonant state equations (1) and (2), magnetizing current increases linearly,  $D_1$  zero-current cuts off at  $t_1$ , the progress of resonance is ended and ZCS of  $D_1$  is realized.

$$v_{C_r}(t) = V_{in}' - (V_{in}' - V_{C_{r,0}}) \cos \omega_r(t - t_0) - Z_r I_o \sin \omega_r(t - t_0) \quad (1)$$

$$i_{L_r}(t) = I_o - I_o \cos \omega_r(t - t_0) + (V_{in}' - V_{C_{r,0}}) \sin \omega_r(t - t_0) / Z_r \quad (2)$$

Where  $V_{Cr0}$  is the initial voltage of  $C_r$ , and  $V_{in}'$  is the induction voltage of the secondary winding when  $Q$  turns on.

Mode 2 [ $t_1$ - $t_2$ ]: The magnetizing current continues to increase linearly, the load energy is provided by  $C_r$ ,  $C_r$  discharging linearly until  $Q$  turns off.

Mode 3 [ $t_2$ - $t_3$ ]: The resonant capacitor  $C_r$  continues to discharge, the flyback part begins to work, magnetizing inductor  $L_m$  demagnetizing and the transformer resets at  $t_3$ .

Mode 4 [ $t_3$ - $t_4$ ]: The magnetizing inductor  $L_m$  begins to resonant with the parasitic capacitor of  $Q$  and provides the condition for  $Q$ 's valley switching.

Through the operation mode analysis in FR-DCM mode, we can get the conclusion that the proposed converter can both realize ZCS of  $D_1$  and valley switching of  $Q$ , which is beneficial for efficiency improvement.

The expression of the output voltage of resonant forward and flyback can be found in the previous literature, as shown in (3) ~ (6).

$$\text{FR:} \quad V_{o1\_FR} = V_{in} \frac{N_2}{N_1} \quad (3)$$

$$\text{PR:} \quad V_{o1\_PR} = V_{in} \frac{N_2}{N_1} - V_{in} I_o \left[ \frac{Z_r(1 - \cos(\omega_r D T_s))}{\omega_r T_s \sin^2 \theta} - \frac{(1-D)^2 T_s}{2C_r} \right] \quad (4)$$

$$\text{DCM:} \quad V_{o2\_DCM} = \frac{V_{in}^2 D^2}{2L_m f_s I_o} \quad (5)$$

$$\text{CCM:} \quad V_{o2\_CCM} = V_{in} \frac{N_3}{N_1} \frac{D}{1-D} \quad (6)$$

Then we can obtain the voltage gain of the proposed converter in different modes by getting the voltage gain of resonant forward part and flyback part respectively:

$$\text{FR-CCM:} \quad V_o = V_{in} \cdot \left( \frac{N_2}{N_1} + \frac{N_3}{N_1} \cdot \frac{D}{1-D} \right) \quad (7)$$

$$\text{FR-DCM:} \quad V_o = V_{in} \cdot \frac{N_2}{N_1} + \frac{V_{in}^2 D^2}{2L_m f_s I_o} \quad (8)$$

$$\text{PR-DCM:} \quad V_o = V_{in} \frac{N_2}{N_1} + \frac{V_{in}^2 D^2}{2L_m f_s I_o} - I_o \left[ \frac{Z_r(1 - \cos(\omega_r D T_s))}{\omega_r T_s \sin^2 \theta} - \frac{(1-D)^2 T_s}{2C_r} \right] \quad (9)$$

$$\text{PR-CCM:} \quad V_o = V_{in} \cdot \left( \frac{N_2}{N_1} + \frac{N_3}{N_1} \cdot \frac{D}{1-D} \right) - I_o \left[ \frac{Z_r(1 - \cos(\omega_r D T_s))}{\omega_r T_s \sin^2 \theta} - \frac{(1-D)^2 T_s}{2C_r} \right] \quad (10)$$

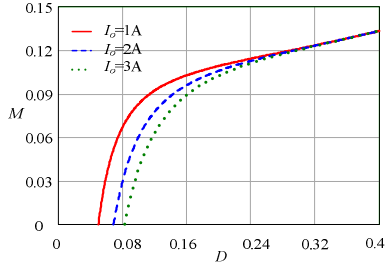


Fig.3 Fixed frequency voltage gain characteristic

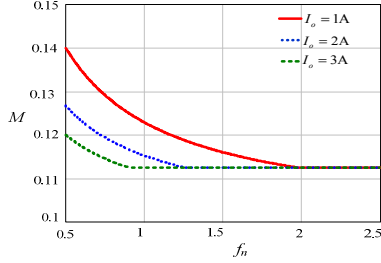


Fig.4 Variable frequency voltage gain characteristic

Fig.3 and Fig.4 illustrate the voltage gain  $M$  characteristics of the proposed converter where  $M=V_o/V_{in}$ . Under fixed frequency condition, the resonant forward part operates in the PR mode if  $D$  is relatively small, and the voltage gain  $M$  rises rapidly with the increase of  $D$ . The resonant forward part enters FR mode with constant gain as  $D$  continues to rise, then the output voltage is completely regulated by the flyback part. For variable frequency condition (with a constant  $D$ ), once the converter enters FR-CCM mode at a certain frequency, the gain of the flyback is only related to  $D$ . The voltage gain  $M$  is no longer varies with the switching frequency in FR-CCM mode.

The characteristics analysis reveals that the proposed converter has the following advantages: (1) Compactness; (2) High efficiency due to the realizing of ZCS for  $D_1$  and valley-switching for  $Q$ ; (3) Most power is transmitted by resonant forward part which can improve the efficiency, and the flyback part realizes the voltage regulation and reset of transformer while delivering a small amount of power.

### III. DESIGN AND CONTROL OF THE PROPOSED CONVERTER

#### A. Power allocation

The power allocation between forward part and flyback part is determined by their output voltage respectively. We can get the power allocation as follow:

$$\frac{P_{o1\_FR}}{P_{o2\_CCM}} = \frac{U_{o1\_FR}}{U_{o2\_CCM}} = \frac{K_1}{K_2} \cdot \frac{1-D}{D} \quad (11)$$

or

$$\frac{P_{o1}}{P_{o2\_DCM}} = \frac{U_{o1\_FR}}{U_{o2\_DCM}} = K_1 \cdot \frac{2L_m I_o f_s}{V_{in} D^2}$$

where  $K_1=N_2/N_1$ ,  $K_2=N_3/N_1$ . As shown in equation (11), different from the FR-CCM mode, the power allocation is determined by  $K_1$ ,  $D$ , and  $f_s$  in FR-DCM mode.

#### B. Voltage Rating And Current Rating Analysis

As shown in Fig.2(b), the voltage rating and current rating of  $D_1$  and  $Q$  is related to the resonant progress between  $L_r$  and  $C_r$ . the resonant impedance  $Z_r$  and resonance shift angle  $\theta$  are defined respectively as:

$$\omega_r = 1/\sqrt{L_r C_r}, Z_r = \sqrt{L_r/C_r}, \theta = \arctan[(I_o Z_r)/(V_{in}' - V_{C_{r0}})] \quad (13)$$

The  $I_r$  and  $V_r$  can be defined and simplified as:

$$I_r = \sqrt{I_o^2 + (V_{in}' - V_{C_{r0}})^2 / Z_r^2}, V_r = \sqrt{I_o^2 Z_r^2 + (V_{in}' - V_{C_{r0}})^2} \quad (14)$$

$$I_r = I_o / \sin \theta, V_r = (I_o Z_r) / \sin \theta \quad (15)$$

Then, the expression of voltage and current rating of  $D_1$  and  $Q$  can be simplified as follow:

$$V_{D1\_pk} = V_{in} \cdot K_1 + \frac{I_o Z_r}{\tan \theta} + \frac{V_{in}^2 D^2}{2L_m I_o f_s} \cdot \frac{K_1}{K_2}, \quad (16)$$

$$I_{D1\_pk} = I_o + \frac{I_o}{\sin \theta}$$

$$V_{Q\_pk} = V_{in} + V_{o2} / K_2, I_{Q\_pk} \approx (I_o + I_r) \cdot K_1 \quad (17)$$

$D_1$  reaches its peak voltage  $V_{D1\_pk}$  when  $Q$  turn-off. The variation of  $V_{D1\_pk}$  can be ignored from  $t_1$  to  $t_2$ . So,  $V_{D1\_pk}$  and  $I_{D1\_pk}$  can be expressed as (16). Ignoring both the resonance between the leakage and the parasitic capacitance and exciting current, we can get the voltage stress and current stress of  $Q$  in (17). It can be found that the voltage stress of  $D_1$  and  $Q$  can be reduced by increasing  $K_2$ .

#### C. Power Loss Analysis

When converter operates in DCM mode, we can calculate the turn-on loss  $P_{Q\_on}$ , conduction loss  $P_{Q\_cond}$  and turn-off loss  $P_{Q\_off}$  use the following equations:

$$P_{Q\_on} = \frac{1}{2} C_{oss(on)} \cdot (V_{in} - V_{o2} / K_2)^2 \cdot f_s \quad (18)$$

$$P_{Q\_cond} = I_{Q\_rms}^2 \cdot R_{DS(on)} = K_1^2 \cdot I_{D1\_rms}^2 \cdot R_{DS(on)} \quad (19)$$

$$P_{Q\_off} = \frac{1}{2} (V_{in} + V_{o2} / K_2) \cdot I_{d\_off} \cdot (t_{chg} + t_f) \cdot f_s \quad (20)$$

Where  $C_{oss(on)}$  is the equivalent output capacitance of  $Q$ ,  $I_{d\_off}$  is the current in  $Q$  when  $Q$  is switched off,  $t_{chg}$  is the junction capacitor charging time of the switch, and  $t_f$  is the time of the current down when the switch is switched off.

For winding loss:

$$P_{Cu\_fbk} = I_{D2\_rms}^2 \cdot r_{fbk} \cdot N_3 = I_{D2\_rms}^2 \cdot r_{fbk} \cdot N_1 \cdot K_2 \quad (21)$$

$$P_{Cu\_fwd} = I_{D1\_rms}^2 \cdot r_{fwd} \cdot N_2 = I_{D1\_rms}^2 \cdot r_{fwd} \cdot N_1 \cdot K_1 \quad (22)$$

$$P_{Cu\_p} = I_{p\_rms}^2 \cdot r_p \cdot N_1 = I_{D1\_rms}^2 \cdot r_p \cdot N_1 \cdot K_1^2 \quad (23)$$

Where  $P_{cu\_fbk}$ ,  $P_{cu\_fwd}$ ,  $P_{cu\_p}$  represent the copper loss of flyback winding, forward winding and primary winding respectively.  $I_{D2\_rms}$ ,  $I_{D1\_rms}$ ,  $I_{p\_rms}$ ,  $r_{fbk}$ ,  $r_{fwd}$ ,  $r_p$  represent their RMS-currents and equivalent resistors. The resonant forward part delivers the most power which means that  $I_{D1\_rms}$  is much larger than  $I_{D2\_rms}$ , therefore the overall effect of increasing  $K_2$  is to reduce the copper loss of the transformer. Through analysis the influence of turns ratio on efficiency, we can optimize the efficiency by using the method shown in Fig 5, and get the optimal turns ratio allocation by trade-off between the switching loss and the winding loss.

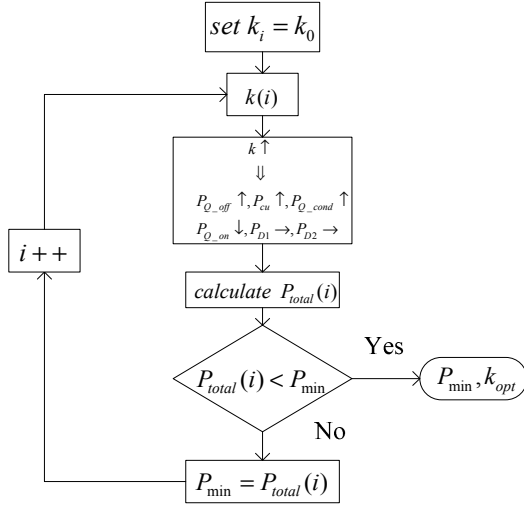


Fig.5 Efficiency optimization flow chart

#### D. Design and control of the converter

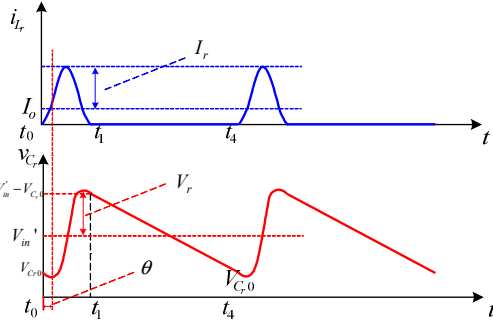


Fig.6 Key waveforms of the resonant forward part

According to the previous analysis, in order to realize both the ZCS of  $D_1$  and valley switching of  $Q$ , the proposed converter has to operate in FR-DCM mode, so, derivation of the condition for FR-DCM is necessary :

$I_{Lr}$  come to 0 at  $t_1$ :

$$I_r \sin(\omega_r t_1 - \theta) + I_o = 0 \quad (24)$$

During  $t_1$  to  $t_4$ ,  $C_r$  discharging linearly:

$$(2V'_m - V_{C0}) - V_{C0} = \frac{I_o}{C_r} (T_s - t_1) \quad (25)$$

Substituting equation(13), (15) and (25) into equation(24), then we can get the express of  $D_{min1}$  :

$$\cos(\omega_r t_1) - \frac{T_s - t_1}{2Z_r C_r} \sin(\omega_r t_1) - 1 = 0 \Rightarrow D_{min1} \quad (26)$$

Where  $D_{min1}$  stands for the critical  $D$  for realizing ZCS.

In order to ensure the converter operate in DCM mode, the duty cycle  $D$  and the switching frequency  $f_s$  also need to meet the constraint conditions:

$$I_o \leq \frac{V_{in} D(1-D)}{2L_m f_s} \cdot \frac{N_1}{N_3} \quad (27)$$

So, we can get the condition for operating in DCM:

$$D_{min2} = \frac{1 - \sqrt{1 - \frac{8I_o f_s L_m N_3}{V_{in} N_1}}}{2} \quad (28)$$

Where  $D_{min2}$  stands for the critical  $D$  for realizing valley switching.

A compound control method based on  $D_{min} \cdot f_s$  control, which ensures the achievement of ZCS and valley switching, is proposed in this paper, as showed in Fig 7. The condition of ZCS and valley switching is determined in (26) and (28). As shown in Fig 8, a constant on-time controller is used to guarantee ZCS and valley switching. Closed loop control is realized by frequency modulation.

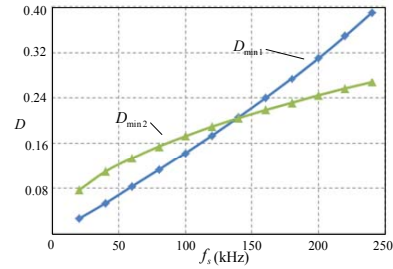


Fig.7  $D_{min} \cdot f_s$  control curve

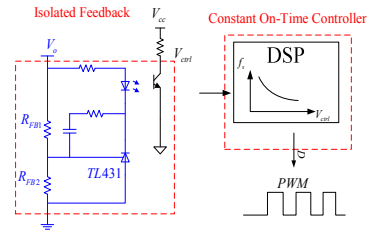


Fig.8 Control scheme

#### IV. EXPERIMENTAL VERIFICATION

A prototype with 400V input 48V /150W output is fabricated to verify the analysis. Two different turns ratios are

chosen for comparison as shown in Tab.3. Fig.10-Fig.12 illustrate the comparison experimental results.

TABLE I. TWO FEASIBLE TURNS RATIO FOR T

	$N_1$	$N_2$	$N_3$	$K_1$	$K_2$
Scheme A	44	4	2	1:11	1:22
Scheme B	36	4	1	1:9	1:36

A. Realizing of ZCS and valley switching

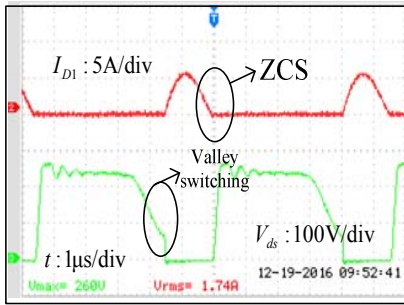


Fig.9  $I_{D1}$ ,  $V_{ds}$  in FR-DCM

Fig.9 shows the achieving of ZCS for the  $D_1$  and valley switching for  $Q$  in FR-DCM.

B. Comparison of scheme A and B

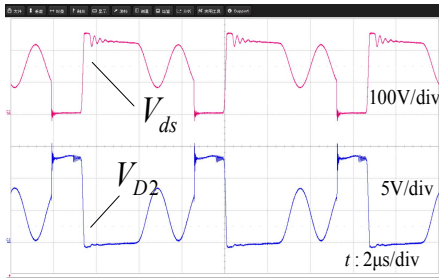


Fig.10 (a)  $V_{D2}$ ,  $V_{ds}$  for scheme A

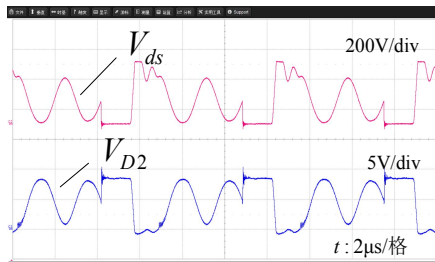


Fig.10 (b)  $V_{D2}$ ,  $V_{ds}$  for scheme B

As shown in Fig.10(a) and Fig.10(b), when  $K_2$  is reduced, the voltage stress of the flyback diode decreases while the voltage stress of the switch increases which agrees well with the theoretical analysis.

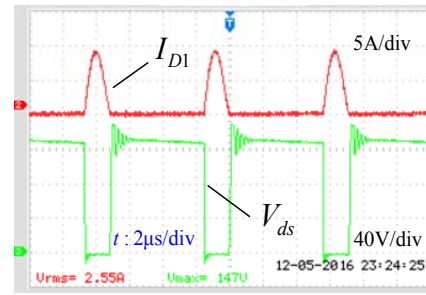


Fig.11 (a)  $I_{D1}$ ,  $V_{ds}$  for scheme A

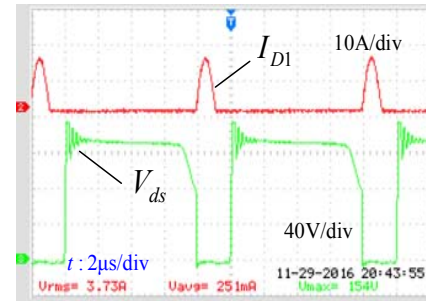


Fig.11 (b)  $I_{D1}$ ,  $V_{ds}$  for scheme B

As shown in Fig.11(a) and Fig.11(b), the reduction of  $K_2$  makes the converter easier to enter DCM mode but results in a larger current stress for  $D_1$ .

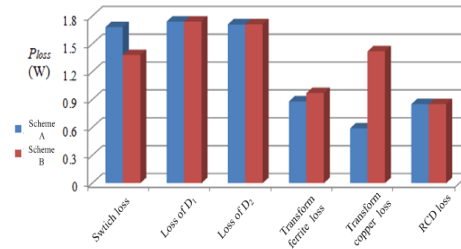


Fig.12  $I_{D1}$ ,  $V_{ds}$  for scheme A

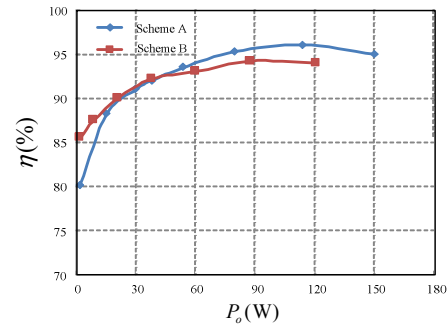


Fig.13  $I_{D1}$ ,  $V_{ds}$  for scheme B

From Fig.12 and Fig.13, we can know that B has higher efficiency than A, with the highest efficiency of 96% at 120W. However, the decrease of switch frequency increases the RMS

current of the secondary, resulting in more copper loss. Experimental results agree with the analysis very well and testify the proposed converter has the advantage of high efficiency.

## V. CONCLUSION

This paper proposes a resonant forward-flyback converter with the concepts of  $\Sigma$ /sigma topology and magnetic integration. The characteristics of the proposed converter are analyzed in detail including the operating principles in different operation modes, the output gain, the ZCS conditions and the power distribution between forward part and flyback part. Besides, this paper also studies the influence of transformer's turns ratios on component stress and power loss. A minimum duty cycle control strategy is proposed to guarantee ZCS of forward diode and valley switching. Finally, a 150 W prototype is constructed to verify the validity of the analysis and the proposed control strategy

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