

# An Evolutionary Method to Achieve the Maximum Efficiency Tracking with Multi-Objective Optimization Based on the Genetic Algorithm

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**Abstract**—A genetic algorithm based method to optimize efficiency of a power converter during running process is proposed in this paper. Compared with the conventional PWM, PFM and multi-mode control techniques, both the duty cycle and the switching frequency are regulated by the proposed method. Benefit from this multi-objective optimization, the maximum efficiency of the converter at a specific load can be approached by choosing and evolving the operating points adaptively. Critical issues, such as the input current sensing, the electrical stress limiting of the power devices and the error compensation of the fitness value, are investigated in order to implement the proposed algorithm. A digital controlled Boost converter based on a microcontroller is built to verify the effectiveness of the algorithm. According to the comparison with conventional control techniques, the peak efficiency with genetic algorithm optimization is 2% higher, and the light load efficiency is optimized over 10%.

**Keywords**—Efficiency optimization, Genetic algorithm, Digital control, Boost converter.

## I. INTRODUCTION

High efficiency is one of the most urgent demands of the power converters [1-3]. Unfortunately, in modern power converters, the current pulse width modulation (PWM) and pulse frequency modulation (PFM) techniques both have drawbacks, for instance, the unnecessarily high switching frequency when the load current decreases. Neither of these two modulation techniques reaches the maximum efficiency over the entire load range [4-5].

In order to decrease the energy waste, maximum efficiency tracking over the entire load range becomes concerned.

Multi-mode control, which is usually a combination of PWM, PFM and burst mode according to the varies load, is applied to improve the efficiency [6-8]. However, complexity of designing is greatly increased by the pre-modeling and pre-training. Also, maximum efficiency tracking is still a doubt.

In fact, there is only one control variable at a time, either the duty cycle or the switching frequency, for the conventional PWM, PFM, and multi-mode control techniques. For instance, in PWM control, every steady-state is a reflection of one single duty cycle  $t_{ON}/T_S$  because of the fixed frequency. Also, steady-state in PFM control is regulated by frequency, for the constant

on-time. When  $[t_{ON}, T_S]$  becomes a solution of steady-state,  $V_O=g(t_{ON}, T_S)$  is a 2-D curve in the  $\{t_{ON}, T_S, V_O\}$  space. In this condition, maximum efficiency tracking is quite difficult because of the restricted operating point.

Since one steady-state  $V_O$  can be achieved by infinite solutions  $[t_{ON}, T_S]$  as long as  $t_{ON}/T_S$  is constant, maximum efficiency tracking can be achieved by finding the most efficient  $[t_{ON}, T_S]$  according to the load. Distinguish from the existing methods which require pre-modeling and complex algorithm, genetic algorithm is an easy way to track the maximum efficiency by evolving continuously [9]. Genetic algorithm (GA) is the most widely used evolution algorithm for the simple fitness, selection and mutation procedure [10-11]. With GA-optimization, finding the maximum efficiency turns to be seeking the best solution in a 3-D plane  $V_O=g(t_{ON}, T_S)$ .

This paper proposes a new consideration to optimize the efficiency of power converter based on GA, which employs efficiency as fitness value and switching frequency as the gene. Furthermore, critical issues, such as the input current sensing, the electrical stress limiting of the power devices and the error compensation of the fitness value, are investigated in order to implement the proposed algorithm.

The paper is organized as follows. Section II describes operating principle and algorithm of a Boost converter with a GA-optimization loop; Section III discusses the efficiency calculation, compensation and the design notes of the converter; and finally, a prototype is built and tested to verify the proposed GA-optimization in Section IV.

## II. BOOST CONVERTER WITH GENETIC ALGORITHM

As illustrated in Fig.1, two digital feedback loops are adopted for GA based efficiency optimization in a Boost converter. A voltage mode feedback loop with a PI controller regulates the output voltage  $V_O$ . Meanwhile, an extra GA feedback loop is employed to optimize the efficiency. The input current  $I_{IN}$  and output current  $I_O$  are sensed by resistors  $R_{CS1}$  and  $R_{CS2}$ , respectively.

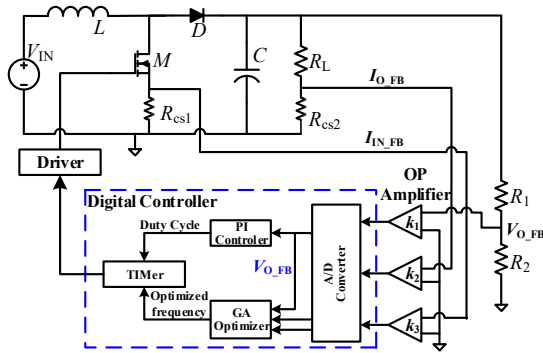


Fig. 1 Boost converter with dual loops

In the dual loop Boost converter, both switching frequency  $f_s$  and on-time  $t_{ON}$  are variables to determine the  $V_O$ . The GA feedback loop is configured to adjust the  $f_s$  of the converter, while duty cycle  $d_{ON}=t_{ON}/f_s$  is determined by the voltage feedback loop.

Flow chart and the algorithm of the digital controller in  $T_n$  (represents for the  $n$ th period) are illustrated in Fig.2 and Fig.3, respectively. The internal program consists of 3 parts, including calculation in the main loop, voltage regulator & current bias sample in interrupt 1 and input current capture in interrupt 2. As Fig.2 shows, the calculated  $d_{ON(n+1)}$  based on  $V_{O(n)}$  regulates  $V_{O(n+1)}$ .

The detailed procedure of the  $f_{s(n+1)}$  optimization is illustrated in Fig.3. In order to ensure the effect of the optimization, the GA loop would not operate until  $V_O$  becomes stable. Steady-state is defined by the error of  $V_O$  during  $m$  continuous periods satisfy

$$\left| k_1 \frac{R_2}{R_1 + R_2} V_{O(m)} - V_{O\_REF} \right| < V_{O\_REF} \cdot 10\% \quad (1)$$

In equation (1),  $k_1$  represents for the coefficient of the Operational amplifier;  $V_{O\_REF}$  represents for the internal reference. When equation (1) is satisfied, GA loop starts to optimize the  $f_s$  until a maximum number of iteration is reached.

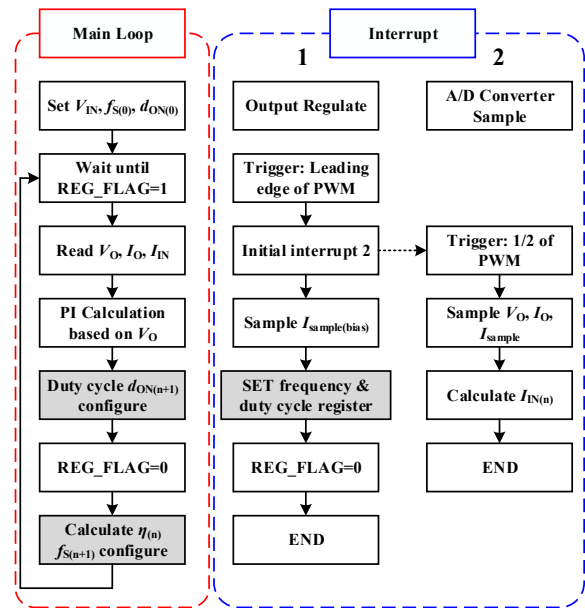


Fig. 2 Flow chart of the control program

Assume the input voltage  $V_{IN}$  is constant and has been defined in the digital controller, the efficiency  $\eta$  of the Boost converter is chosen as the fitness value of the GA-optimization, which is calculated by the microcontroller as

$$\eta = \frac{V_O I_O}{V_{IN} I_{IN}} \quad (2)$$

In a single GA-optimization trial, a series of random individual  $[t_{ON}, T_S]_{1...n}$  which satisfy equation (1) are applied to the Boost converter during  $n$  periods, and  $\eta_{1...n}$  are evaluated in next period with equation (2). After abandoning 2 most inefficient solutions, the calculated  $\eta_{1...n-2}$  are summed as a total fitness

$$\eta_{sum} = \sum_{k=1}^{n-2} \eta_k \quad (3)$$

The next generation is generated randomly according to the ratio of each individual in the total fitness

$$P_j = \frac{\eta_j}{\eta_{sum}} \quad (4)$$

The method of generating consists of mutating and interbreeding. After several generations, the fitness value of each individual  $[t_{ON}, T_S]_{1...n}$  becomes equal, most individuals in this generation reaches the maximum efficiency. One of the best individual is picked with a typical load current and stored as  $[I_O, t_{ON}, T_S]$ . When the  $I_O$  is close to previous optimized condition, the individual is recalled and applied.

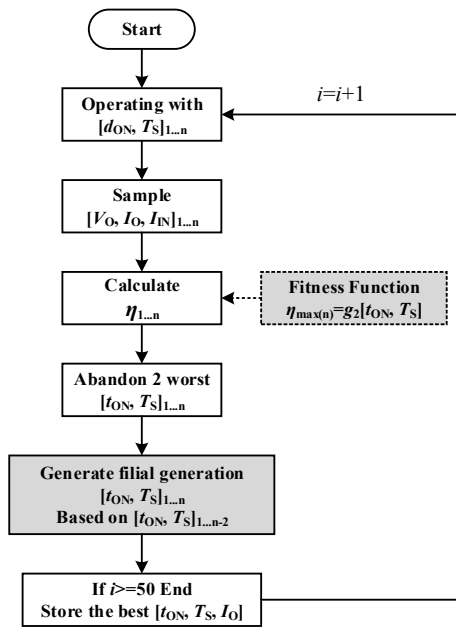


Fig. 3 Algorithm of GA-optimization loop

### III. SAMPLE AND CONTROL STRATEGY

#### a) Input current sensing

The DC output values  $V_O$  and  $I_O$  in equation (2) are easy to sample. Unfortunately,  $I_{IN}$  is difficult to sample directly because of the sawtooth waveform, as shown in Fig.4. Thus, a special method should be considered based on the operating principle of the Boost converter.

In a Boost converter, the inductor  $L$  is charged during on-time  $t_{ON}$  of  $M$ . Thereby, the average input current can be reflexed by the bias and peak current of  $I_D$ . However, capturing the accurate peak value of  $I_D$  seems impossible because of the delay of both the power stage and instruction cycle of the microcontroller. Luckily, in a digital power converter, duty cycle is often decided in the previous period, so that capturing the input current at  $t=0$  and  $t=0.5t_{ON}$  of each period is much easier. The input current sensing strategy is demonstrated in Fig.4.

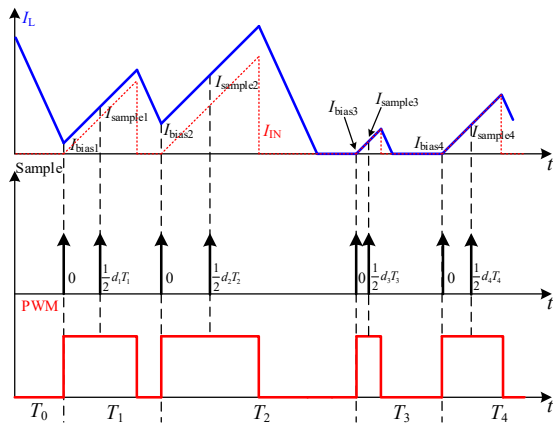


Fig. 4 Time diagram of the input current sensing

According to Fig.4,  $I_{IN}$  can be expressed as

$$I_{IN} = \frac{t_{ON}}{T_S} (I_{sample} - I_{bias}) \quad (5)$$

In equation (5),  $I_{bias}$  is captured by the interrupt 1,  $I_{sample}$  is captured by the interrupt 2,  $t_{ON}$  and  $T_S$  are determined by the PWM module and initialized by interrupt 1.

An advantage of this strategy is eliminating the influence of the delay. Assume that the sample delay is  $\Delta t$ , the error  $\Delta i$  between sampled current and actual current is

$$\Delta i = \frac{V_{IN} - V_O}{L} \Delta t \quad (6)$$

The errors are canceled when delays of  $I_{sample}$  and  $I_{bias}$  are the same, thus an accurate  $I_{IN}$  can be sampled.

According to these considerations, a precise input current is sample and calculated for evaluating the fitness value  $\eta$ .

#### b) Individual limitations during the GA-Optimization

Stable output voltage/current is the most important performance of a power converter, thus every single individual  $[t_{ON}, T_S]$  of GA-optimization should ensure the stability of  $V_O$ . Theoretically,  $V_O$  of Boost converter is stable when

$$V_O = \frac{T_S}{T_S - t_{ON}} V_{IN} \quad (7)$$

However, in an actual converter, several rules should be satisfied, such as the current stress on the power devices  $M$  and  $D$  should be safe; the magnetic core of  $L$  cannot be saturated; and the most important is the loop must be stable.

The reliability of the  $M$ ,  $D$  and  $L$  is ensured by a limited  $[t_{ON}, T_S]$  range. For instance, during the entire load current range,  $I_{IN}$  should be restricted by

$$\frac{L \cdot \Delta I_{IN}}{N \cdot A_e} < B_{max} \quad (8)$$

In equation (8),  $N$ ,  $A_e$  and  $B_{max}$  are pre-defined turns, core area and maximum magnetic flux density, respectively. According to the voltage-second balance of the Boost converter,  $f_s$  is also limited by

$$f_s > \frac{V_{IN} (V_O - V_{IN})}{V_O N A_e B_{max}} \quad (9)$$

Thus, the reliability of the converter is ensured.

The stability of the voltage feedback loop is also concerned. The parameters of digital PI controller are computed in advance according to load resistance and the lowest frequency calculated in equation (9).

#### c) Fitness value calculation and compensation

The fitness value, which is the calculated efficiency, is the most important parameter in the GA-optimization.

However, the calculated efficiency cannot exactly match the measured value, because the accuracy of the internal A/D converter is finite, meanwhile, noise in the circuit is unavoidable. Thus the calculated efficiency should be compensated in order to reduce the error.

Different  $I_{IN}$  are calculated ( $I_{cal}$ ) and measured ( $I_{cal}$ ) under several typical  $f_s$  with the loop opened. Matlab is used to

process the data  $[f_s, I_{real}, I_{cal}]$ . In the end, a 3-D graph is drawn to reveal the approximate relationship between calculation and measurement with minimum error, as shown in Fig.5.

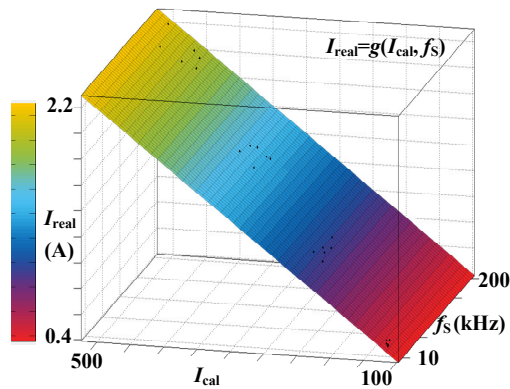


Fig.5 Curve fitting with Matlab to compensate the error

According to the 3-D image shown in Fig.5,  $f_s$  does not influence the error, thus a linear coefficient is employed to compensate the error during the fitness value evaluation.

#### IV. EXPERIMENTAL RESULTS

A prototype is built to verify the proposed method, as shown in Fig.6. Parameters of the Boost converter is listed in Table 1.

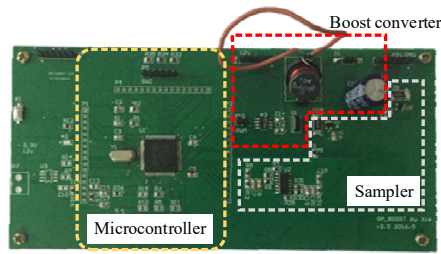


Fig.6 Photograph of the prototype

Table 1 Parameters of the Boost converter

Parameter/Component	Value
Input voltage, $V_{IN}$	6V
Output voltage, $V_O$	12V
Output current, $I_O$	1A
Inductor, $L$	100 $\mu$ H(Coilcraft)
Output capacitor, $C$	330 $\mu$ F
Switching frequency, $f_s$	200kHz
Power MOSFET, $M$	IRFU024N(Infineon)
Rectifier diode, $D$	UF4007(Fairchild)
Voltage sensor, $R_1/R_2$	22k $\Omega$ /1k $\Omega$
Current sensor, $R_{CS1}, R_{CS2}$	10m $\Omega$
Closed loop gain $k_1/k_2/k_3$	2/20/20
Voltage amplifier	OPA4350UA(TI)
Current amplifier	INA193(TI)
Microcontroller	STM32F407VGT6(ST)
Gate-drive chip	IR4427(Infineon)

Fig.7 (a)(b) show the waveform of  $I_{IN}$  capturing both under heavy and light load conditions. The PWM and Sample signals are output of the microcontroller. The color of the arrow illustrates the sampling time. It is proved that the proposed current sensing strategy is effective no matter whether the

converter is under CCM or DCM. Also, switching frequency does not influence the accuracy of the sampling.

The output voltage ripple of the converter is illustrated in Fig.8. The steady-state error of  $V_O$  is around 100mV.

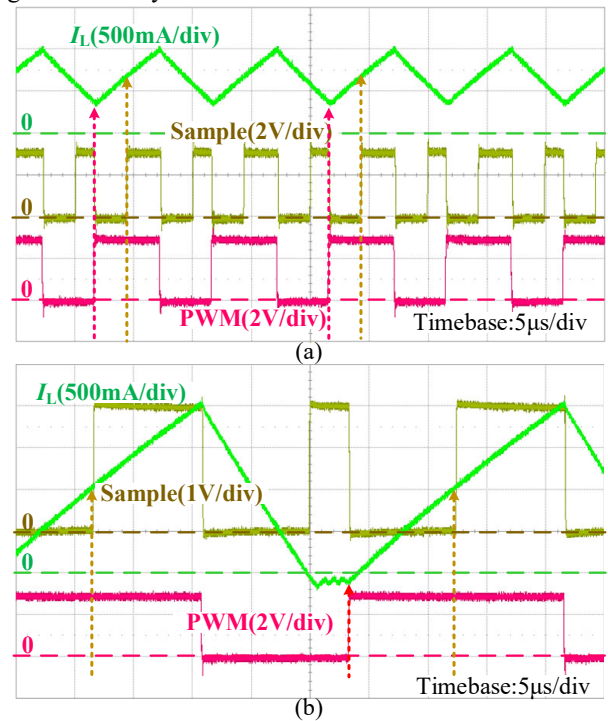


Fig. 1 Input current capturing strategy under (a)CCM heavy load condition; (b)DCM light load condition

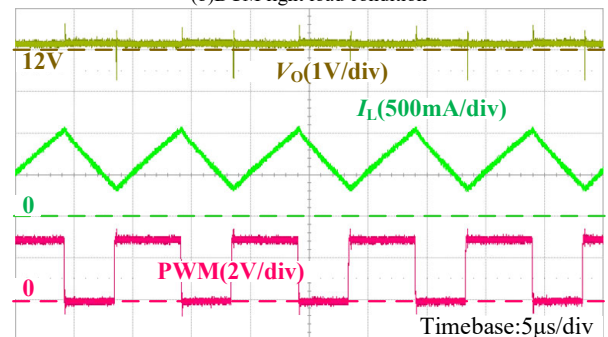


Fig.8 Ripple of the output voltage

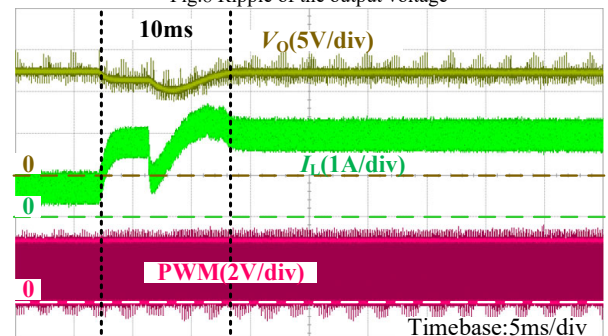


Fig. 9 Waveform during Load transient from 0.1A to 1A

Fig.7 (a)(b) show the waveform of  $I_{IN}$  capturing both under heavy and light load conditions. The color of the arrow illustrates the sampling time. It is proved that the proposed current sensing strategy is effective no matter whether the converter is under CCM or DCM. Also, switching frequency does not influence the accuracy of the sampling.

The output voltage ripple of the converter is illustrated in Fig.8. The steady-state error of  $V_O$  is around 100mV.

Performance of the PI controller is tested, as shown in Fig.9. The transient performance of 10ms is acceptable at quite a low frequency (50kHz).

In the end, efficiency over the entire load range is measured to verify the effect of GA-optimization, under 4 control strategies, PWM control, PFM control, multi-mode control and the GA-optimization, as shown in Fig.10. The peak efficiency with GA-optimization is 2% higher, and the light load efficiency is optimized over 10%.

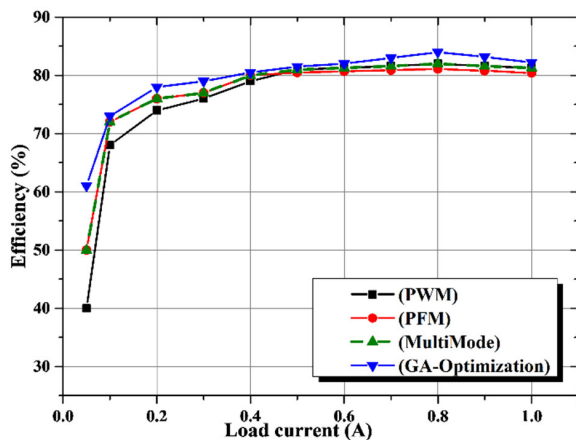


Fig.10 The efficiency comparison of the proposed GA-optimization and other control techniques

According to the test results, the validity of the proposed GA-optimization is proved. What's more, GA-optimization does not require complicated control strategies applied in multi-mode control technique, because of the ability of evolution.

It is expected that the GA-optimization would be used to improve efficiency in other converters, for instance, self-adaptive dead time control in phase leg configurations, and accurate synchronous rectifier driving scheme control.

## V. CONCLUSION

This paper proposes an efficiency optimization method based on GA. The evolutionary GA-optimization improves the efficiency of the converter over the entire load range by choosing and evolving the operating points adaptively. The input current sensing, the electrical stress limiting of the power devices and the error compensation of the fitness value are discussed in order to implement the GA-optimization. A microcontroller based Boost converter with both voltage

feedback loop and GA-optimization loop is realized and evaluated. Experimental results show that accurate current sensing is achieved during all the operating modes of the converter. Compared to those with PWM/PFM/multi-mode control, the Boost converter with GA-optimization has the best efficiency performance over the entire load range.

## ACKNOWLEDGMENTS

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