

# Initial Rotor Position Estimation for Brushless Synchronous Starter/Generators

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**Abstract**—In this paper, an initial rotor position estimation method that is independent of the magnetic saliency is proposed for the main generator (MG) of the brushless synchronous starter/generator (BSSG). The stator of the MG works as a transmitter and the rotor of the MG works as a receiver, i.e., signals are injected into the stator windings and response signals of the field winding are regarded as indicators of the initial rotor position of the MG. Due to the brushless structure, direct measurement of the field winding of the MG is difficult. Thus, a practical approach to estimate the information of the field winding of the MG is proposed in this paper. Then, the initial rotor position of the MG is estimated with signal injection. The effectiveness of this method is verified by experimental results.

## I. INTRODUCTION

The brushless synchronous starter/generator (BSSG), which is highly reliable and inherently safe, is widely adopted by the integrated starter/generator system [1]–[7]. The structure of the three-stage BSSG is shown in Fig. 1. Three machines, a pre-exciter (PE), a main exciter (ME) and a main generator (MG), and a rotating rectifier are mounted on the same shaft.

The initial rotor position of the MG is essential for sensorless start control of the BSSG [8]–[10]. Many initial rotor position estimation methods have been proposed, especially for permanent magnet synchronous motors (PMSMs). The magnetic saliency, an indicator of the rotor position, of the PMSM is usually detected by signal injection. The stator of the PMSM is both a transmitter and a receiver, i.e., signals are injected into the stator windings and response signals of the stator windings are analyzed to estimate the initial rotor position of the PMSM. In general, the magnetic saliency of the PMSM is stable, so the estimation results are reliable. Compared with the PMSM, the magnetic saliency of the MG is variable. Consequently, methods proposed for the PMSM may cause large error when applied to the MG. In [11], the field winding of the electrically excited synchronous machine (EESM) is used for signal detection, i.e., the stator is the transmitter and the rotor is the receiver. Initial rotor position

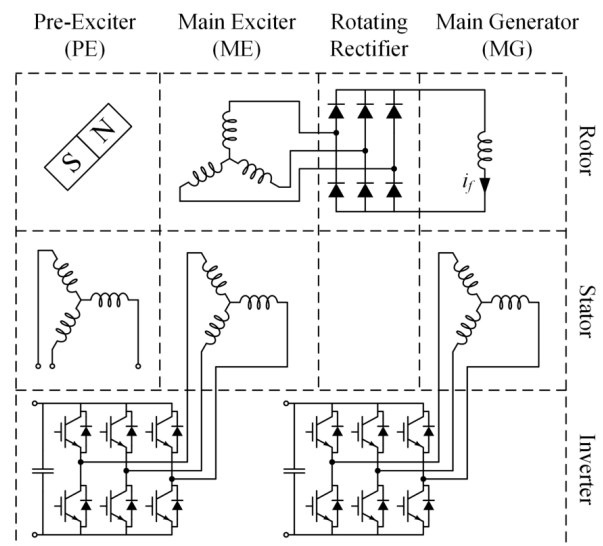


Fig. 1. Structure of the three-stage BSSG.

estimation with this transmission direction is independent of the magnetic saliency and proven to be a suitable choice for the EESM [12]. Therefore, this transmission direction is also preferred for the initial rotor position estimation of the MG. However, methods proposed for the EESM cannot be applied to the MG directly, because the brushless structure prevents measurement of the field winding of the MG. To obtain the field winding information of the MG, a method is proposed in [13]. The field current of the MG is calculated with parameters and the rotor position of the ME. Unfortunately, the ME information needed in this method is usually not all available. In [14], when the BSSG is at standstill, the field current of the MG is estimated without knowing the rotor position of the ME. However, parameters of the ME are still needed and

only simulation results are presented. As the rotor windings of the ME are connected with the rotating rectifier and cannot be measured, it is difficult to provide all the parameters needed in [14].

According to the measurability of parameters of the ME, a practical approach to estimate the field winding information of the MG is proposed in this paper. Then, signals are injected into the stator of the MG and response signals of the field winding are estimated and analyzed to detect the initial rotor position of the MG. An experimental platform is built to verify this method.

## II. ESTIMATION OF THE FIELD WINDING INFORMATION OF THE MG AT STANDSTILL

The excitation system, shown in Fig. 2, of the BSSG consists of the ME, the field winding of the MG and the rotating rectifier. In Fig. 2,  $i_{esA}$ ,  $i_{esB}$ ,  $i_{esC}$  are the stator currents,  $i_{era}$ ,  $i_{erb}$ ,  $i_{erc}$  are the rotor currents,  $i_f$  is the field current of the MG, and  $\theta_{er}$  is the rotor position.  $\theta_{er} = \theta_{e0} + \omega_{er}t$ , where  $\theta_{e0}$  is the initial rotor position and  $\omega_{er}$  is the rotor electrical angle velocity. According to the mathematical model of the ME, the rotor  $d$ - and  $q$ -axis currents are

$$i_{erd} = \frac{2}{3M_{esr}} \left[ \int (u_{es\alpha} - R_{es}i_{es\alpha})dt - L_{es}i_{es\alpha} \right] \quad (1)$$

$$i_{erq} = \frac{2}{3M_{esr}} \left[ \int (u_{es\beta} - R_{es}i_{es\beta})dt - L_{es}i_{es\beta} \right] \quad (2)$$

where  $R_{es}$  is the stator resistance,  $L_{es}$  is the stator inductance, and  $M_{esr}$  is the mutual inductance.  $i_{era}$ ,  $i_{erb}$ ,  $i_{erc}$  can be derived from the frame transformation

$$\begin{bmatrix} i_{era} \\ i_{erb} \\ i_{erc} \end{bmatrix} = \begin{bmatrix} \cos \theta_{er} & \sin \theta_{er} \\ -\sin(\theta_{er} + \frac{\pi}{6}) & \cos(\theta_{er} + \frac{\pi}{6}) \\ \sin(\theta_{er} - \frac{\pi}{6}) & -\cos(\theta_{er} - \frac{\pi}{6}) \end{bmatrix} \begin{bmatrix} i_{erd} \\ i_{erq} \end{bmatrix} \quad (3)$$

With the method in [13], the field current of the MG is

$$i_f = \frac{|i_{era}| + |i_{erb}| + |i_{erc}|}{2} \quad (4)$$

In equations (1)-(4),  $R_{es}$ ,  $L_{es}$ ,  $M_{esr}$ , and  $\theta_{er}$  are essential to calculate  $i_f$ . At standstill,  $\theta_{er} = \theta_{e0}$ . With  $R_{es}$ ,  $L_{es}$ , and  $M_{esr}$ ,  $i_f$  can be estimated without knowing  $\theta_{e0}$  [14]. Due to the extremely large inductance of the field winding of the MG and the rotating rectifier, the actual  $i_f$  is a dc current with a small amplitude ripple which is six times the frequency of the rotor currents of the ME [9], and this should also be the case with the estimated field current  $i_f^e$  (the superscript  $e$  denotes estimated variables). If  $\theta_{e0}^e$  deviates from  $\theta_{e0}$ , the ripple amplitude of  $i_f^e$  will increase. Therefore,  $i_f^e$  with the smallest ripple amplitude is the correct estimation result and the corresponding  $\theta_{e0}^e$  can be used to estimate  $i_f$  at standstill. The same smallest ripple amplitude will be detected at six  $\theta_{e0}^e$  with  $60^\circ$  interval, and the actual initial rotor position of the

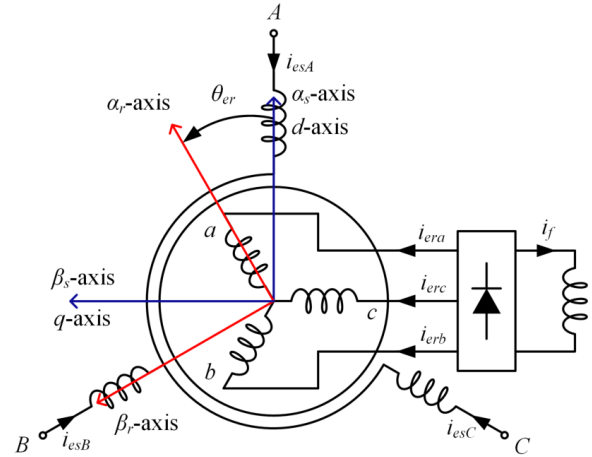


Fig. 2. Schematic of the excitation system of the BSSG.

ME is one of them but cannot be identified. Fortunately,  $i_f$  can be estimated correctly with any one of the six positions [14].

Among the three parameters,  $R_{es}$  can be measured from the stator of the ME. To measure  $L_{es}$ , the BSSG can be driven to the same speed with the rotating magnetic field of the stator of the ME. Then, the currents of the rotor windings of the ME are zero and  $L_{es}$  can be measured with just currents and voltages of the stator windings of the ME. Since the rotor windings of the ME are connected with the rotating rectifier and difficult to measure, obtaining  $M_{esr}$  is a challenging job. From equations (1)-(4), it can be observed that  $M_{esr}$  is a scale factor multiplied in  $i_f^e$ . Thus, equations (1)-(4) are rewritten as equations (5)-(8). It should be mentioned that flux linkage variables in equations (5)-(8) are just symbols for calculation and may do not have clear physical meanings. With measured  $R_{es}$  and  $L_{es}$  of the ME, the field winding information, defined as  $\psi_f$ , of the MG can be estimated from equations (5)-(8) without knowing  $\theta_{e0}$  when the BSSG is at standstill.  $i_f^e$  and  $\psi_f^e$  share same features and the only difference between them is a scale factor  $M_{esr}$ .

$$\psi_{erd} = i_{erd}M_{esr} = \frac{2}{3} \left[ \int (u_{es\alpha} - R_{es}i_{es\alpha})dt - L_{es}i_{es\alpha} \right] \quad (5)$$

$$\psi_{erq} = i_{erq}M_{esr} = \frac{2}{3} \left[ \int (u_{es\beta} - R_{es}i_{es\beta})dt - L_{es}i_{es\beta} \right] \quad (6)$$

$$\begin{bmatrix} \psi_{era} \\ \psi_{erb} \\ \psi_{erc} \end{bmatrix} = \begin{bmatrix} \cos \theta_{er} & \sin \theta_{er} \\ -\sin(\theta_{er} + \frac{\pi}{6}) & \cos(\theta_{er} + \frac{\pi}{6}) \\ \sin(\theta_{er} - \frac{\pi}{6}) & -\cos(\theta_{er} - \frac{\pi}{6}) \end{bmatrix} \begin{bmatrix} \psi_{erd} \\ \psi_{erq} \end{bmatrix} \quad (7)$$

$$\psi_f = \frac{|\psi_{era}| + |\psi_{erb}| + |\psi_{erc}|}{2} \quad (8)$$

### III. INITIAL ROTOR POSITION ESTIMATION OF THE MG

The schematic of the MG is shown in Fig. 3, where  $i_A, i_B, i_C$  are the stator currents,  $u_A, u_B, u_C$  are the stator voltages,  $u_f$  is the field voltage,  $\theta_0$  is the initial rotor position,  $\theta_0^e$  is the estimated initial rotor position, and  $\Delta\theta_0$  is the difference between  $\theta_0$  and  $\theta_0^e$ . When the BSSG is at standstill, the  $d$ -axis and the  $q$ -axis are decoupled, and only the  $d$ -axis is coupled with the field winding. When the sinusoidal voltage signal is injected into the  $d^e$ -axis, the current ripple with the same frequency will be induced in  $i_f$  and this information will also be included in  $\psi_f$ . When the resistive voltage drop is ignored, the induced ripple of  $\psi_f$ , defined as  $\psi_{fh}$ , can be approximately expressed as

$$\psi_{fh} = \frac{3M_{af}M_{esr}}{3M_{af}^2 - 2L_dL_{ff}} \frac{U_h}{2\pi f_h} \sin(2\pi f_h t) \cos(\Delta\theta_0) \quad (9)$$

where  $M_{af}$  is the mutual inductance,  $L_d$  and  $L_{ff}$  are the  $d$ -axis inductance and the field winding inductance,  $U_h$  and  $f_h$  are the amplitude and frequency of the injected sinusoidal voltage signal. From (9), the smaller the  $\Delta\theta_0$ , the higher the amplitude of  $\psi_{fh}$ . Therefore, the amplitude of  $\psi_{fh}$  can be used as the indicator for  $\theta_0$ . When  $\Delta\theta_0 = 0^\circ$  or  $180^\circ$ , the amplitudes of  $\psi_{fh}$  are the same. This  $180^\circ$  ambiguity can be eliminated by step signal injection. If a step voltage is injected, a sudden decrease of  $\psi_f$  will appear when  $\Delta\theta_0 = 0^\circ$ , while a sudden increase of  $\psi_f$  will appear when  $\Delta\theta_0 = 180^\circ$ . Therefore,  $\theta_0$  equals  $\theta_0^e$  with the biggest amplitude of  $\psi_{fh}$  when the sinusoidal voltage is injected and a sudden decrease of  $\psi_f$  when the step voltage is injected.

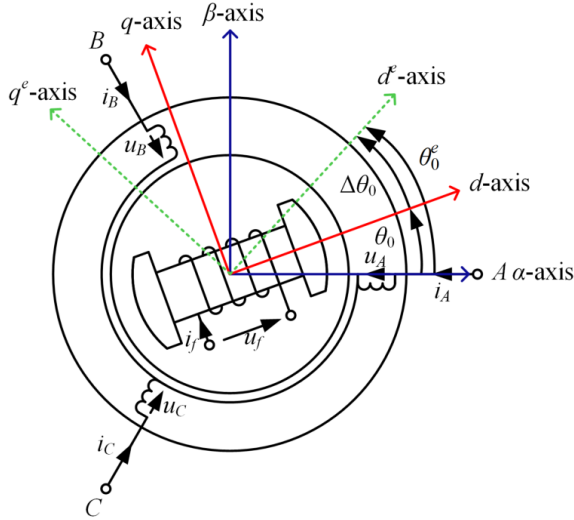


Fig. 3. Schematic of the MG of the BSSG.

### IV. EXPERIMENTAL RESULTS

The experimental setup is shown in Fig. 4. The BSSG consists of a three-phase wound-rotor induction machine (ME) and an electrically excited synchronous machine (MG). The rotor windings of the ME and the field winding of the MG

are connected by a three-phase rectifier. Control algorithms are implemented on a RT-LAB system.

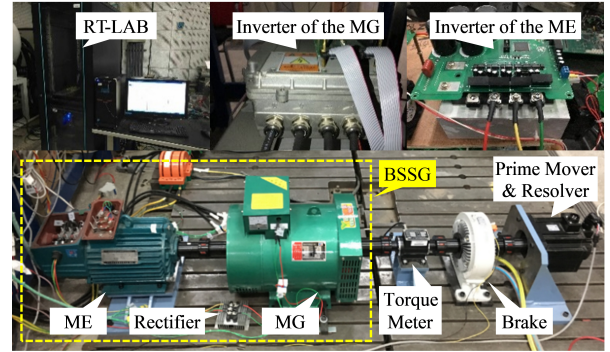


Fig. 4. Experimental setup.

$R_{es}$  of the ME is about  $4.72 \Omega$ . To measure  $L_{es}$  of the ME, the BSSG is driven to the same speed with the rotating magnetic field of the stator of the ME. Then, with measured currents and voltages of the stator windings of the ME,  $L_{es}$  is estimated by the least square method. The estimation results are shown in Fig. 5 and  $L_{es}$  is about  $0.29 \text{ H}$ .

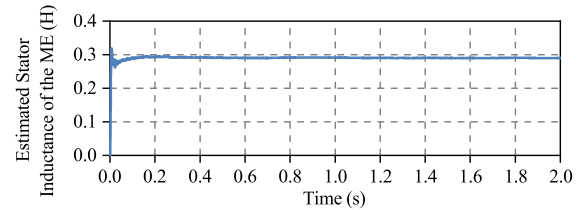


Fig. 5. Estimation results of the stator inductance of the ME.

To obtain  $\theta_{e0}^e$  that is used to estimate the field winding information of the MG, a set of balanced  $70 \text{ V}/50 \text{ Hz}$  three-phase voltages is applied to the stator windings of the ME. Then,  $\theta_{e0}^e$  from  $0^\circ$  to  $360^\circ$  are used to estimate  $\psi_f$  with equations (5)-(8). Fast Fourier transform is performed to obtain the amplitude of the  $300 \text{ Hz}$  ripple of  $\psi_f^e$  at different  $\theta_{e0}^e$ , and the results are shown in Fig. 6. It can be observed that six positions,  $7.5^\circ, 67.5^\circ, 127.5^\circ, 187.5^\circ, 247.5^\circ$  and  $307.5^\circ$ , are with the same smallest amplitude of the  $300 \text{ Hz}$  ripple. Fig. 7 shows that all the six positions have the same estimation result of  $\psi_f$ , so any one of them can be used to estimate  $\psi_f$ .

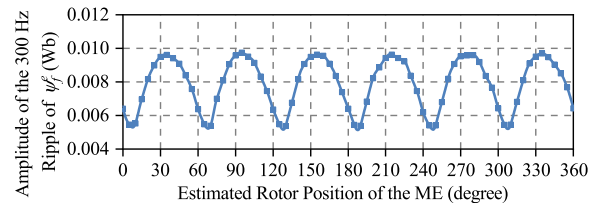


Fig. 6. Amplitude of the  $300 \text{ Hz}$  ripple of  $\psi_f^e$  at different  $\theta_{e0}^e$

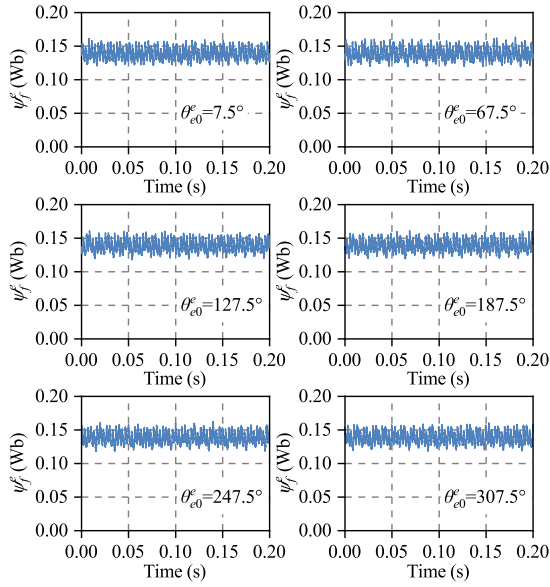


Fig. 7.  $\psi_f^e$  at the six  $\theta_{e0}$  with the same smallest amplitude of the 300 Hz ripple.

A 40 V/500 Hz sinusoidal voltage is injected into the  $d^e$ -axis to estimate the initial rotor position of the MG. When  $\theta_0^e$  are from  $0^\circ$  to  $360^\circ$ , the amplitude of  $\psi_{fh}$ , which is the 500 Hz ripple of  $\psi_f^e$ , is shown in Fig. 8 (a). The largest amplitude of  $\psi_{fh}$  occurs at two positions,  $122^\circ$  and  $302^\circ$ . Then, a 30V step voltage is injected at the two positions and the results are shown in Fig. 8 (b) and (c). The sudden decrease of  $\psi_f^e$  indicates  $122^\circ$  is correct. The actual initial rotor position of the MG is  $120^\circ$ , so the estimation error is about  $2^\circ$ . This estimation accuracy can meet the requirement of start control of the BSSG.

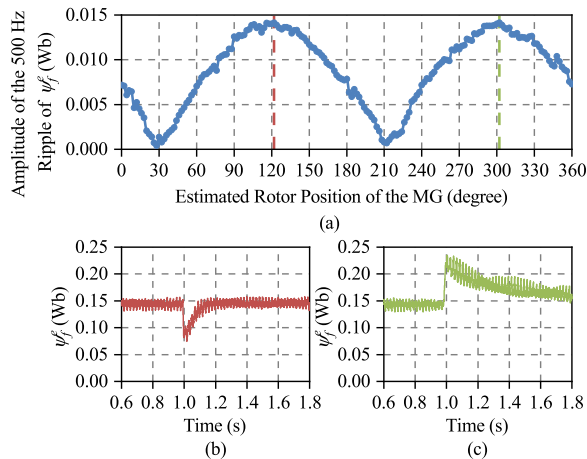


Fig. 8. (a): Amplitude of the 500 Hz ripple of  $\psi_f^e$  at different  $\theta_0^e$ . (b):  $\psi_f^e$  at  $122^\circ$ . (c):  $\psi_f^e$  at  $302^\circ$ .

## V. CONCLUSION

This paper has proposed a method to estimate the initial rotor position of the MG by signal injection. The stator and the rotor of the MG are the transmitter and the receiver respectively. The field winding information of the MG is estimated from the ME with measured parameters of the ME. The validity of the proposed method is verified by experimental results.

## ACKNOWLEDGMENT

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